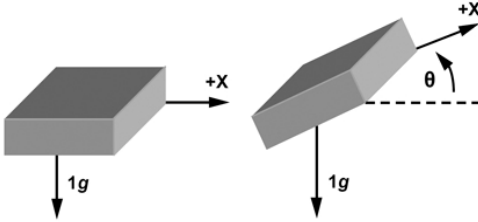


Application Note 273 Using BioNomadix Tri-axial Accelerometer as a Tilt Sensor Inclinometer

Tilt angle or inclination sensing uses measurements of gravity, and its trigonometric projection on the axes of a tri-axial accelerometer (such as [BN-ACCL3](#)), to determine tilt angle in all three spatial dimensions (X, Y and Z). The following picture illustrates a single axis tilt measurement using a single acceleration measurement.

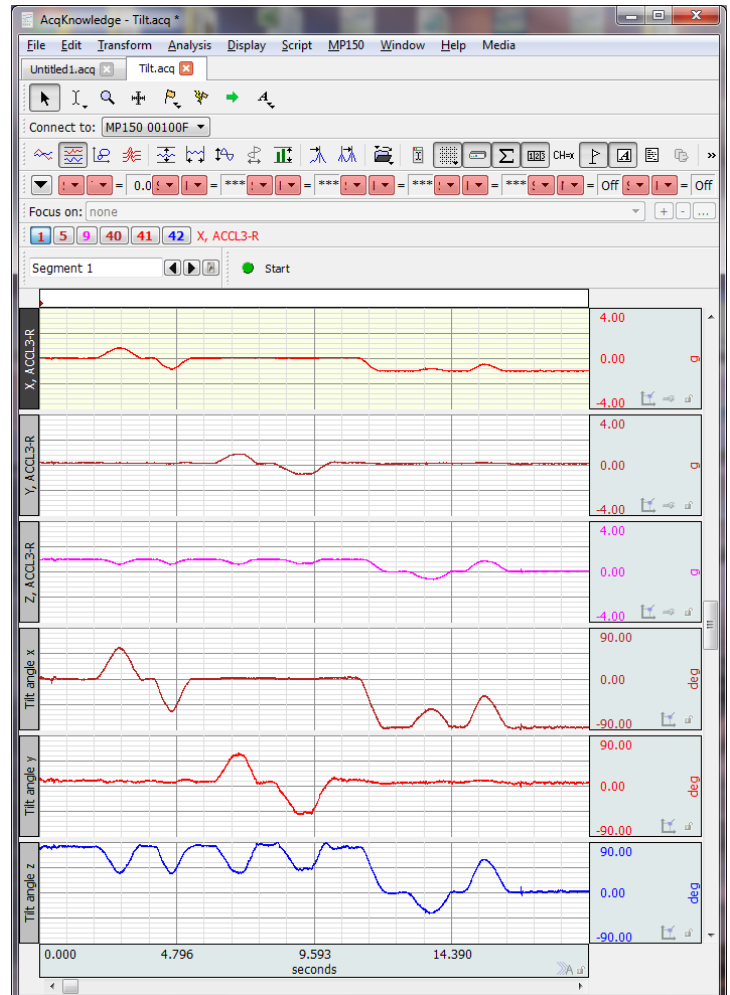
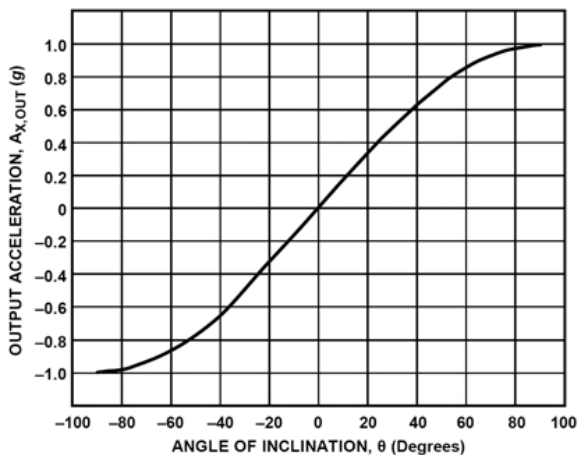


In this case, the following formula applies:

$$A_x = 1g * \sin(\theta_x)$$

Namely, the acceleration measured along the X-axis (A_x) is equal to the gravity vector ($1g$) multiplied by the sine of the tilt angle with respect to the X-axis (θ_x).

The following graph illustrates the output acceleration reported by the X-axis of a tri-axial accelerometer, as the accelerometer is tilted from -90 degrees to +90 degrees, assuming 0 degree tilt is parallel to the orientation of the X-axis. Note the point of maximum sensitivity is when the accelerometer is near 0 degrees tilt angle (angle of inclination).



Collected Data – Acceleration and Tilt Angles for X, Y and Z Axis

For a single axis tilt measurement, using just the X-axis of the accelerometer, the following formula can be employed to calculate tilt angle or angle of inclination (θ_x) from the acceleration measured along the X-axis:

$$\theta_x = \arcsin(A_x)$$

However, this above formula has associated problems: 1) Assumes alignment with plane of gravity; 2) Variable sensitivity based upon tilt angle (note flattening at ± 90 degrees). To remove these factors, all the axis of the accelerometer can be used. The following calculations can be setup in the AcqKnowledge calculation channels to calculate up to 3 orientations of tilt simultaneously, in real-time, using the BN-ACCL or any other BIOPAC tri-axial accelerometer, such as TSD109C2.

$$\begin{aligned} \text{X-axis tilt: } \theta_y &= \arctan(A_x / \sqrt{A_y^2 + A_z^2}) \\ \text{Y-axis tilt: } \theta_x &= \arctan(A_y / \sqrt{A_x^2 + A_z^2}) \\ \text{Z-axis tilt: } \theta_z &= \arctan(A_z / \sqrt{A_x^2 + A_y^2}) \end{aligned}$$

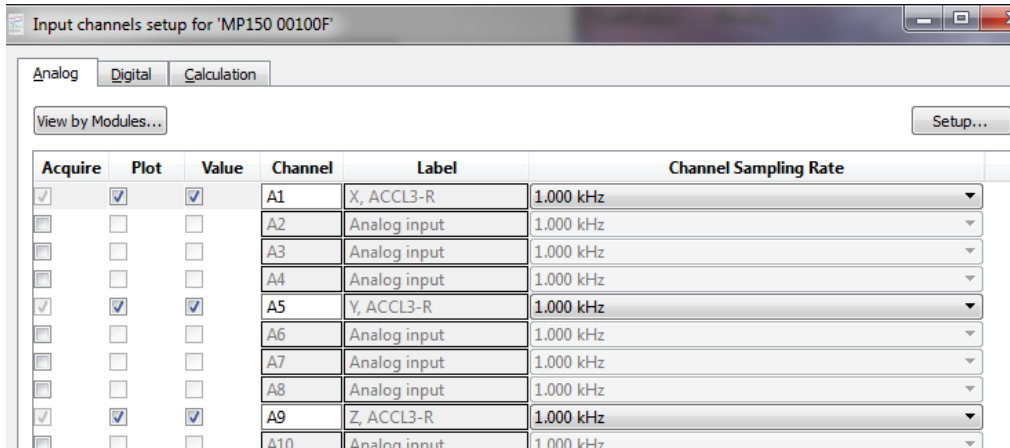
These measurements are performed in radians, so to convert to degrees, use the following conversion factor:

$$\text{Pi (radians)} = 180 \text{ degrees}$$

$$\begin{aligned} \text{X-axis tilt degrees: } \theta_x &= (180/\text{Pi}) * \arctan(A_x / \sqrt{A_y^2 + A_z^2}) \\ \text{Y-axis tilt degrees: } \theta_y &= (180/\text{Pi}) * \arctan(A_y / \sqrt{A_x^2 + A_z^2}) \\ \text{Z-axis tilt degrees: } \theta_z &= (180/\text{Pi}) * \arctan(A_z / \sqrt{A_x^2 + A_y^2}) \end{aligned}$$

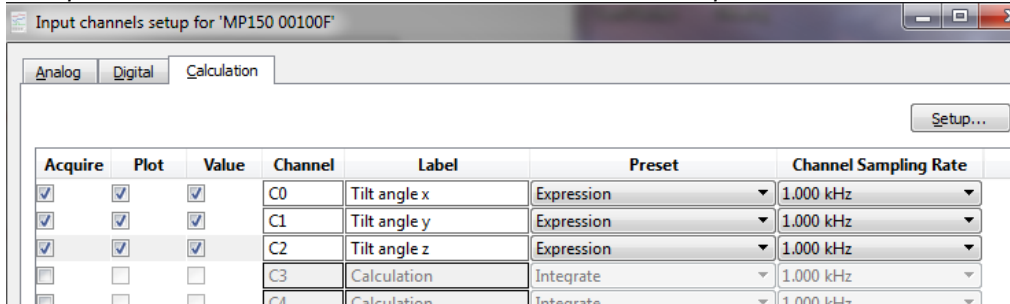
AcqKnowledge Setup

1) Set up Analog Channels A1 X, A5 Y, A9 Z:

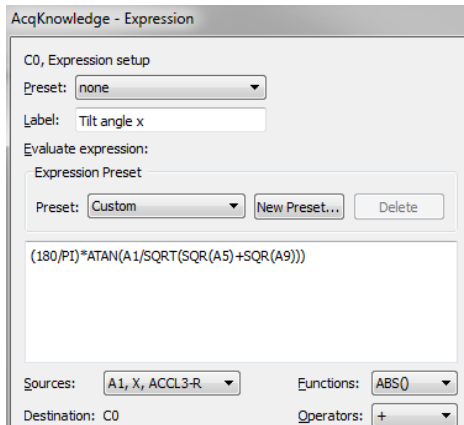


Input Channel Setup for BN-ACCL

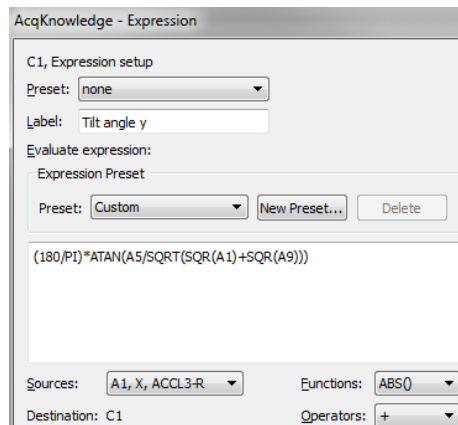
2) Set up Calculation Channels C0 X, C1 Y, C2 Z and enter Expressions for each:



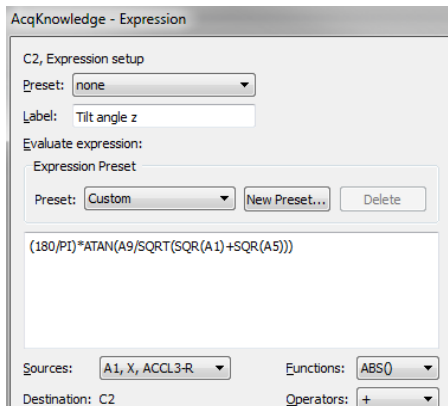
Calculation Channel Setup for BN-ACCL – Tilt Measurement



Expression Setup for Tilt Angle X (θ_x)



Expression Setup for Tilt Angle Y (θ_y)



Expression Setup for Tilt Angle Z (θ_z)